New Method for Increase of Noise Immunity of GPS Navigation Systems

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Abstract—The paper is devoted to the developed new method for decrease of effect of specially formed jamming signals on functioning of GPS navigation system. The effect of hindering signal of jamming type transmitted by technical means of adversary side is considered. Generation of jamming signal of relevant frequency and sufficient power by adversary is carried out by the aim to reach the condition of non-possibility of receipt of GPS signals. The suggested method is based on basic equation of antenna theory, that is Friis equation. According to Friis equation the power of signal received by antenna of moving object with defined gain coefficient can be calculated upon transmission of signal from target objects antenna with known gain coefficient. The new parameter calculated by integration of Friis formula on passed distance supposing static character of jamming signal source position is suggested. On the basis of research of suggested parameter the target functional is formed taking into account the motionless position of jamming signal generator and non-changeable motion direction of moving object toward target containing jamming signal generator. The possible strategies for changing the jamming signal power on transition of object on route are also taken into account. It is shown that suggested parameter is of extremum feature upon proportional or non proportional variation of gain coefficients of antennas of object and jamming signal generator: upon proportional variation the suggested parameter reaches the minimum and upon inverse identity maximum. Taking into account the extremum feature of suggested parameter the method and algorithm for decrease of effect of jamming signal on functioning of GPS navigation systems of similar technical constructions are developed.

Index Terms—Friis equation, antenna, atmosphere, error, navigation system, optimization, functional.

I. INTRODUCTION

As it was noted in [1], one of fundamental equations of theory of communication using antennas is Friis transmission equation. The Friis transmission equation make it possible to calculate the power received by first antenna with gain coefficient $G_1$ upon transmission of signal from the second antenna with gain coefficient $G_2$. In this case the distance between antennas equals to $R$, and transmission is carried out at wavelength $\lambda$ (Fig.1).

\[
P_R = \frac{P_T \cdot G_T \cdot G_R \cdot \lambda^2}{(4\pi R^2)}
\]

where: $P_T$—power of transmitted signal; $P_R$—power of received signal; $G_T$—gain coefficient of transmitting antenna; $G_R$—gain coefficient of receiving antenna.

According to Friis law the power of received signal could be determined as

\[
P_R = P_T + G_T(\theta_T, \phi_T) + G_R(\theta_R, \phi_R) + 
\left[ \frac{\lambda}{4\pi R} \right]^2 \cdot \left[ 1 - |F_T|^2 \right] \cdot \left[ 1 - |F_R|^2 \right] \cdot |a_T \cdot a_R|^2 \cdot e^{-\alpha R}
\]

where: $(\theta_T, \phi_T)$—irradiation direction of transmitting antenna; $(\theta_R, \phi_R)$—receipt direction of receiving antenna; $F_T$—reflection coefficient of transmitting antenna; $F_R$—reflection coefficient of receiving antenna; $a_T$, $a_R$—polarization vectors of transmitting and receiving antennas, accordingly; $\alpha$—coefficient of attenuation of atmosphere.

It should be noted that formula (1) is simplified one i.e. the effect of atmospheric attenuation is not taken into account here. More strict formula for calculation of $P_R$ taking into account the atmospheric attenuation is following [2-4]:

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attacking signals are differentiated: hindering jamming and false control spoofing signals. In first case the aim is to do impossible receiving of GPS signals by generation of signal of same frequency and sufficient power. In the second case aim is forming false control signal not differing from real signal. For example, in 2001 the technical services of Iran carry out the forced controlled landing of drone RQ—170 Sentinel, forming relevant control signal [2].

As it is noted in [5-6], GPS navigation system is based on receipt of signals from height 20000 km, which lead to low power of received signals. Due to this reason GPS receivers are subjected the effect of different type noises. If signal/noise ratio surpasses 25 dB, GPS is not capable to receive (C/A) code, and if said ratio equals to 55dB the navigation accuracy code (P) is loosed [7-8]. In order to increase the noise immunity of navigation system such methods as multi-frequency systems (GPS, GALILEO, GLONAS); filtration at a single frequency; method of adaptive antennas by using of linear set antennas with maximum gain in direction to satellites and minimum gain in direction of noise generator [5, 9-10]. Next in this article we explain the theoretical basics of suggested new method for increasing the noise immunity of GPS navigation systems based on utilization of adaptively controlled antenna. The Friis formula (1) may be written as

$$ P_R = \frac{A \cdot G_T \cdot G_R}{R^2} $$

where

$$ A = \frac{P_T \cdot \lambda^2}{16 \pi^2} = C_1 = \text{const} $$

(4)

Next we consider the situation when dependence $G_T = f(R)$ exists, also the distance $R$ between receiver and noise generator is variable parameter. Let us to consider following suggested integrated parameter

$$ \chi_1 = \int_0^{R_M} P_R dR = \int_0^{R_M} \frac{A \cdot G_T \cdot G_R}{R^2} dR $$

(5)

where: $R_M$—maximum length of distance.

Physical meaning of parameter $\chi$ is following. Assume that there is a moving object equipped with GPS/INS navigation system and static noise generator, installed at target which should be reached by moving object (it is may be guided aviation bomb). In equation (5) $R$ is distance determined as $R = R_o - R_x$; where $R_o$—initial distance between the target (i.e. noise generator) and moving object; $R_x$—current distance between them.

It is determined that the parameter $G_R$ should be controlled on $R$, while the law of control of $G_T$ is not known, but can be revealed and calculated during flight of object toward target. Two variants of adaptive variation of $G_R$ depending on $G_T$ are considered:

1. $G_R = G_T$ (6)
2. $G_R = G_1 - G_T$, $G_1 = \text{const}$. (7)

Next we assume that the aim of noise generator is synthesis of utmost hindering effective noise signals within limits of energy recourses of noise generator. As noise generation is carried out at all interval of variation of $R$, beginning from zero up to $R_M$ within limits of said energy resources for variation of antennas gain coefficient, the second integrated parameter could be suggested

$$ \chi_2 = \int_0^{R_M} G_T(R) dR = C_2 $$

(8)

Where $C_2 = \text{const}$.

Taking into account equations (5) and (8) we can compose following equation of non-conditional variation optimization

$$ \chi_1 = \chi_1 + \lambda \cdot \chi_2 = \int_0^{R_M} \frac{AG_T(R)G_R(R)}{R^2} dR + \lambda \left[ \int_0^{R_M} G_T(R) dR - C_2 \right] $$

(9)

We should select one of equations (6) and (7), which upon some $\chi_1$ would reach the minimum. According to Euler-Lagrange equation the optimum function $G_R(R)$ should meet following condition
\[
d\left\{ \frac{A \cdot G_T(R) \cdot G_R(R)}{R^2} + \lambda \cdot G_T(R) \right\} \frac{1}{dG_T(R)} = 0
\]  \hspace{1cm} \text{(10)}

From condition (10) taking into account (6) we get
\[
\frac{2AG_T(R)}{R^2} + \lambda = 0
\]  \hspace{1cm} \text{(11)}

From (11) it is derived that
\[
G_T(R) = \frac{-\lambda \cdot R^2}{-2A}
\]  \hspace{1cm} \text{(12)}

Taking into account formulas (8) and (12) we get
\[
\lambda_2 = -\int_0^{R_m} \frac{\lambda \cdot R^2}{2A} dR = -\frac{\lambda \cdot R_m^3}{6A} = C_2
\]  \hspace{1cm} \text{(13)}

From equation (13) we have
\[
\lambda = -\frac{6AC_2}{R_m^3}
\]  \hspace{1cm} \text{(14)}

Taking into account formulas (11) and (14) we found
\[
\frac{2A \cdot G_T(R)}{R^2} = \frac{6A \cdot C_2}{R_m^3}
\]  \hspace{1cm} \text{(15)}

Finally, from (15) we get
\[
G_T(R) = \frac{3C_2 \cdot R^2}{R_m^3}
\]  \hspace{1cm} \text{(16)}

Thus, upon condition (16) the target functional (9) reaches its maximum. In order to check up the type of extremum it is sufficient to calculate the second derivative of integrant in (9) on $G_T(R)$ and to be assured that it reaches a positive that is extremum is of maximum type.

Now we study the extremum feature of functional (9) taking into account condition (7). In this case the functional (9) could be written as:
\[
\lambda_3 = \int_0^{R_m} A \cdot G_T(R) \cdot \left[ C_1 - G_T(R) \right] dR + \lambda \int_0^{R_m} G_T(R) dR - C_2
\]  \hspace{1cm} \text{(17)}

According to Euler-Lagrange equation the functional (17) reaches its extremum upon function $G_T(R)$, which meet following condition
\[
d\left\{ \frac{A \cdot G_T(R) \cdot \left[ C_1 - G_T(R) \right]}{R^2} + \lambda \cdot G_T(R) \right\} = 0
\]  \hspace{1cm} \text{(18)}

From condition we get (18)
\[
\frac{AC_1 - 2AG_T(R)}{R^2} + \lambda = 0
\]

From equation (19) we get:
\[
G_T(R) = \frac{\lambda \cdot R^2 + AC_1}{2A}
\]

(20)

Taking into account formulas (8) и (20) we found
\[
\int_0^R \left[ \frac{\lambda R^2 + AC_1}{2A} \right] dR = C_2
\]

From equation (21) we find that
\[
\lambda = \left( \frac{C_2 - \frac{1}{C_2} \cdot R_m}{C_2} \right) \cdot 6A
\]

(22)

Taking into account equations (19) и (22) we get
\[
\frac{AC_1 - 2A \cdot G_T(R)}{R^2} = \left( \frac{C_1 \cdot R_m}{2} - C_2 \right) \cdot 6A
\]

From equation (23) it may be found that
\[
G_T(R) = \frac{C_1}{2} - \frac{3R^2}{R_m^2} \cdot \left( \frac{C_1 \cdot R_m}{2} - C_2 \right)
\]

(24)

Thus upon condition (24) the target functional (17) reaches its extremum. As it was noted above, in order to determine the type of extremum the second derivative of integrant in (17) should be calculated and its sign should be determined. The negative sign of said derivative would prove that the target functional reaches its maximum.

Taking into account aforesaid following method for increasing the noise immunity of GPS navigation system is suggested. According to suggested method the system equipped with GPS navigation system should be provided with two antennas, with coefficients of gain
\[
G_{R_1}(R) = G_{R}(R)
\]

(25)

\[
G_{R_2}(R) = C_1 - G_{R}(R)
\]

(26)

In this case the antenna with gain coefficient \( G_{R_2}(R) \) is designated for joint work with noise generators antenna. The aim of such joint work is adaptive change of \( G_{R_2}(R) \) in such manner that to reach the maximum of target functional
\[
\chi_4 = \int_0^R \frac{P_T \cdot G_{R_2}(R) \cdot G_T(R) \cdot \lambda^2}{(a\pi R)^2} dR + \left[ \int_0^R G_T(R) dR - C_2 \right]
\]

(27)

Maximum of functional (27) is reached by adaptive variation of \( G_{R_2}(R) \), studying dynamics of \( G_T(R) \) and providing for inverse dynamics of variation of \( G_{R_2}(R) \).

As it was shown above in this case the effect of noise generator on antenna with gain coefficient \( G_{R_2}(R) \) would be maximum and it effect on antenna with gain coefficient \( G_{R_1}(R) \) would be minimum.

As regards the authenticity of limitation condition (8), imposed on gain coefficient of noise generators antenna the graphic interpretation of this condition shown in figure 8 make it possible to interprete condition (8) in the form of three strategies for organization of protection from noise effects:

– At the beginning of tracking cycle, when the distance between tracked object (for example, guided aviation bomb) and noise generator is maximum noise of...
maximum power should be generated, (curve 1 at the fig.8.)

– At the middle of moving objects tracking cycle the noise of maximum value should be generated (curve 2 at fig.8).

– On minimum possible distance between between object and noise generator, at the end of tracking cycle the noise of maximum value should be generated. (curve 3 at fig.2).

![Diagram](https://doi.org/10.31871/IJNTR.5.7.12)

Fig.2. Possible curves of variation of $G_T(R)$ at the distance $0—R_{ma}$, in line with accepted strategy for generation of noise signal.

REFERENCES


